

Integrals of Standard Functions

Exponential

$$\begin{aligned}\int e^x dx &= e^x + C & \int \ln(x) dx &= x \ln(x) - x + C \\ \int \frac{1}{x} dx &= \ln(|x|) + C & \int \log_a(x) dx &= \frac{x}{\ln(a)} (\ln(x) - 1) + C \\ \int a^x dx &= \frac{a^x}{\ln(a)} + C\end{aligned}$$

Trigonometric

$$\begin{aligned}\int \sin(x) dx &= -\cos(x) + C & \int \sec(x) dx &= \ln(|\sec(x) + \tan(x)|) + C \\ \int \cos(x) dx &= \sin(x) + C & \int \csc(x) dx &= -\ln(|\csc(x) + \cot(x)|) + C \\ \int \tan(x) dx &= -\ln(|\cos(x)|) + C & \int \frac{1}{\sqrt{a^2 - x^2}} dx &= \sin^{-1}\left(\frac{x}{a}\right) + C \\ \int \cot(x) dx &= \ln(|\sin(x)|) + C & \int \frac{1}{a^2 + x^2} dx &= \frac{1}{a} \tan^{-1}\left(\frac{x}{a}\right) + C \\ \int \sec^2(x) dx &= \tan(x) + C\end{aligned}$$

Hyperbolic

$$\begin{aligned}\int \sinh(x) dx &= \cosh(x) + C & \int \frac{1}{\sqrt{x^2 + a^2}} dx &= \sinh^{-1}\left(\frac{x}{a}\right) + C \\ \int \cosh(x) dx &= \sinh(x) + C & \int \frac{1}{\sqrt{x^2 - a^2}} dx &= \cosh^{-1}\left(\frac{x}{a}\right) + C \\ \int \tanh(x) dx &= \ln(\cosh(x)) + C\end{aligned}$$

Reduction Formulas

$$\begin{aligned}\int \sec^n(x) dx &= \frac{1}{n-1} \sec^{n-2}(x) \tan(x) + \frac{n-2}{n-1} \int \sec^{n-2}(x) dx \\ \int \tan^n(x) dx &= \frac{1}{n-1} \tan^{n-1}(x) - \int \tan^{n-2}(x) dx\end{aligned}$$